

Measurement of the CKM angle φ_1 in $B^0 \rightarrow \overline{D}^{(*)0} h^0$, $\overline{D}^0 \rightarrow K_S^0 \pi^+ \pi^-$ decays with time-dependent binned Dalitz plot analysis

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We report a measurement of the CP violation parameter φ_1 obtained in a time-dependent analysis of $B^0 \rightarrow \bar{D}^{(*)0} h^0$ decays followed by $\bar{D}^0 \rightarrow K_S^0 \pi^+ \pi^-$ decay. A model-independent measurement is performed using the binned Dalitz plot technique. The measured value is $\varphi_1 = 11.7^\circ \pm 7.8^\circ$ (stat.) $\pm 2.1^\circ$ (syst.). Treating $\sin 2\varphi_1$ and $\cos 2\varphi_1$ as independent parameters, we obtain $\sin 2\varphi_1 = 0.43 \pm 0.27$ (stat.) ± 0.08 (syst.) and $\cos 2\varphi_1 = 1.06 \pm 0.33$ (stat.) $^{+0.21}_{-0.15}$ (syst.). The results are obtained with a full data sample of $772 \times 10^6 B\bar{B}$ pairs collected near the $\Upsilon(4S)$ resonance with the Belle detector at the KEKB asymmetric-energy e^+e^- collider.

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I. INTRODUCTION

The study of CP symmetry provides valuable insight into the structure and dynamics of matter from the subatomic to the cosmic scale. CP violation is a necessary ingredient for baryogenesis and explaining the state of matter in the observable Universe [1]. The Standard Model (SM) of particle physics accounts for CP viola-

tion using the mechanism proposed by Kobayashi and Maskawa (KM) [2]. A unitary matrix of quark flavor mixing, referred to as the Cabibbo-Kobayashi-Maskawa (CKM) [2, 3] matrix, encodes this mechanism. The CKM matrix makes charged weak currents non-invariant under CP transformation. The SM does not predict the values of the elements of the CKM matrix, but theoretical predictions estimate that the amount of CP violation in-

roduced by the SM is too feeble to explain the baryon asymmetry of the Universe [4]. Thus, it is important to test the KM mechanism and search for new sources of CP violation.

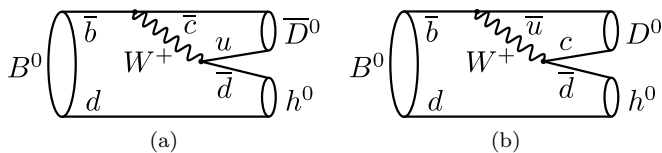


FIG. 1. $\bar{b} \rightarrow \bar{c}u\bar{d}$ transition (a) leading to $B^0 \rightarrow \bar{D}^0 h^0$ decay and $\bar{b} \rightarrow \bar{u}c\bar{d}$ transition (b) leading to $B^0 \rightarrow D^0 h^0$ decay.

Unitarity of the CKM matrix implies several relations among its elements that can be represented as triangles in the complex plane. In particular, the relation formed by the elements of the first and the third columns, referred to as the Unitarity Triangle (UT) [5], is the most accessible for experimental tests.

The CP violation parameter $\varphi_1 = \arg(-V_{cd}V_{cb}^*/V_{td}V_{tb}^*)$, where V_{ij} is an element of the CKM matrix, is one of the angles of the UT¹. The value of $\sin 2\varphi_1$ has been measured precisely in $b \rightarrow c\bar{c}s$ transitions by Belle, BaBar and LHCb [6]. Two discrete ambiguities remain with the known value of $\sin 2\varphi_1$: $\varphi_1 \rightarrow \varphi_1 + \pi$ and $\varphi_1 \rightarrow \pi/2 - \varphi_1$. Currently, no theoretical approach is available to resolve the former ambiguity, but the latter can be resolved by measuring $\cos 2\varphi_1$. Existing measurements of $\cos 2\varphi_1$ in $b \rightarrow c\bar{u}d$ [7, 8] and $b \rightarrow c\bar{c}s$ [9, 10] transitions are much less precise and, in most cases, model-dependent.

Here, we present a model-independent measurement of the angle φ_1 in $b \rightarrow c\bar{u}d$ transitions (Fig. 1a) governing $B^0 \rightarrow \bar{D}^{(*)0}h^0$ decays with subsequent $\bar{D}^0 \rightarrow K_S^0\pi^+\pi^-$ decay², where h^0 is a light unflavored meson. This measurement is based on a data sample twice as large as that used in the previous φ_1 measurement using $B^0 \rightarrow \bar{D}^{(*)0}h^0$ decays at Belle [8]. The technique of a binned Dalitz plot analysis is applied to the φ_1 measurement for the first time.

A. Formalism

This section describes the technique to measure the angle φ_1 at an asymmetric-energy e^+e^- collider operating at center-of-mass (CM) energy near the $\Upsilon(4S)$ resonance [11, 12]. When a pair of neutral B mesons is produced, they oscillate coherently until one decays. Therefore, at the moment of a flavor-specific decay of one of

the B mesons (in the $\Upsilon(4S)$ rest frame), the flavor of the other B meson is fixed. The former B meson is referred to as the *tagging* B meson and the latter as the *signal* B meson. The tagging and signal B mesons decay at proper times t_{tag} and t_{sig} , respectively.

The longitudinal distance Δz along the beam axis between the decay vertices of the signal and tagging B mesons in the lab frame is measured. Since the B mesons are produced almost at rest in the CM frame, their momentum can be neglected and the approximation $\Delta t \approx \Delta z/(c\beta\gamma)$ can be used, where $\Delta t = t_{\text{sig}} - t_{\text{tag}}$ and β and γ are the Lorentz factors of the $\Upsilon(4S)$ parent.

If the amplitudes $\mathcal{A}(B^0 \rightarrow f) \equiv \mathcal{A}_f$ and $\mathcal{A}(\bar{B}^0 \rightarrow f) \equiv \bar{\mathcal{A}}_f$ are non-zero for some final state f , then the distribution of the decay time difference, attributed to the interference of the processes $B^0 \rightarrow f$ and $B^0 \rightarrow \bar{B}^0 \rightarrow f$, is [11]

$$\mathcal{P}(\Delta t) = h_1 e^{-\frac{|\Delta t|}{\tau_B}} \left[1 + \frac{1 - |\lambda_f|^2}{1 + |\lambda_f|^2} \cos(\Delta m_B \Delta t) - \frac{2 \text{Im} \lambda_f}{1 + |\lambda_f|^2} \sin(\Delta m_B \Delta t) \right], \quad \lambda_f = \frac{q \bar{\mathcal{A}}_f}{p \mathcal{A}_f}, \quad (1)$$

where p and q are the coefficients relating the mass and flavor B -meson eigenstates to each other, τ_B is the neutral B meson lifetime (assumed to be the same for both mass eigenstates), Δm_B is the mass difference between the mass eigenstates, and h_1 is a normalizing constant. In the following, we assume the absence of CP violation in mixing and a null CP -violating weak phase in the B meson decay amplitudes:

$$\frac{q}{p} = e^{-i2\varphi_1}, \quad \arg\left(\frac{\bar{\mathcal{A}}_f}{\mathcal{A}_f}\right) = \Delta\delta_f, \quad (2)$$

so that

$$\text{Im} \lambda_f = \left| \frac{\bar{\mathcal{A}}_f}{\mathcal{A}_f} \right| \sin(\Delta\delta_f - 2\varphi_1); \quad (3)$$

here, $\Delta\delta_f$ is the difference in strong phases, which does not change sign under a CP transformation. Consideration of the CP -conjugated process, in which the CP -violating phase φ_1 is replaced by $-\varphi_1$, allows one to distinguish between the weak ($2\varphi_1$) and strong ($\Delta\delta_f$) phases.

For $B^0 \rightarrow \bar{D}^{(*)0}h^0$ decays, the amplitudes \mathcal{A}_f and $\bar{\mathcal{A}}_f$ can be expressed as

$$\mathcal{A}_f = \alpha_B \bar{\mathcal{A}}_D, \quad \bar{\mathcal{A}}_f = \alpha_B \xi_{h^0} (-1)^L \mathcal{A}_D, \quad (4)$$

where ξ_{h^0} is the CP eigenvalue of the h^0 meson, L is the relative angular momentum in the $D^{(*)0}h^0$ system, \mathcal{A}_D ($\bar{\mathcal{A}}_D$) is the D^0 (\bar{D}^0) decay amplitude into the final state f_D , and α_B is a complex coefficient. The charm mixing and possible CP violation in the D meson decays are neglected in Eq. (4). With the existing B -factories statistics, the $B^0 \rightarrow D^0 h^0$ decay amplitude

¹ Another naming convention, β ($\equiv \varphi_1$), is also used in the literature.

² Throughout this paper, the inclusion of the charge-conjugate decay mode is implied unless otherwise stated.

(Fig. 1b) can be neglected with respect to the $B^0 \rightarrow \bar{D}^0 h^0$ decay amplitude (Fig. 1a) because it is suppressed by $|V_{ub}V_{cd}/V_{cb}V_{ud}| \approx 0.02$.

If the state f_D is a CP eigenstate, then the entire state f is CP eigenstate (except for the $\bar{D}^{*0}h^0$ state with a vector h^0 meson) as well and the phase $\Delta\delta_f$ equals 0 or π . This exposes a sensitivity to $\sin 2\varphi_1$ but not $\cos 2\varphi_1$ and provides the best way to measure $\sin 2\varphi_1$ in $b \rightarrow \bar{c}ud$ transitions [13].

The three-body state $f_D = K_S^0\pi^+\pi^-$ is not a CP eigenstate, so the phase $\Delta\delta_f$ is not limited to the values 0 and π . As a consequence, this state provides sensitivity to both $\sin 2\varphi_1$ and $\cos 2\varphi_1$. The amplitude of $D^0 \rightarrow K_S^0\pi^+\pi^-$ decay can be expressed as a function $\mathcal{A}_D(m_+^2, m_-^2)$ of two Dalitz-distribution variables [14], where $m_{\pm} = m(K_S^0\pi^{\pm})$ are the invariant masses. The amplitude $\bar{\mathcal{A}}_D$ of $\bar{D}^0 \rightarrow K_S^0\pi^+\pi^-$ decay can be obtained by transposing the Dalitz variables: $\bar{\mathcal{A}}_D(m_+^2, m_-^2) \equiv \mathcal{A}_D(m_-^2, m_+^2)$. Therefore, the phase difference $\Delta\delta_f$ is a function of the Dalitz variables:

$$\begin{aligned} \Delta\delta_f(m_+^2, m_-^2) &= \arg(\xi_{h^0}(-1)^L) - \Delta\delta_D(m_+^2, m_-^2), \\ \Delta\delta_D(m_+^2, m_-^2) &= \arg\left(\frac{\mathcal{A}_D(m_-^2, m_+^2)}{\mathcal{A}_D(m_+^2, m_-^2)}\right). \end{aligned} \quad (5)$$

For the $f_D = K_S^0\pi^+\pi^-$ final state, the strong phase $\Delta\delta_D$ cannot be measured at each point in the phase space: additional information is necessary. An approach based on an isobar model of the D meson decay amplitude was proposed in Ref. [15] and used in the measurement of the CKM angle φ_1 performed by BaBar [7] and Belle [8]. Alternatively, we use here a method that is independent of the decay model, as described below.

B. Time-dependent binned Dalitz plot analysis

Our measurement is based on the binned Dalitz distribution approach. This idea was proposed in Ref. [16] to measure the CKM angle φ_3 and further developed for several applications in Refs. [17–19]. We extend this approach to measure the angle φ_1 in the time-dependent analysis of $B^0 \rightarrow \bar{D}^{(*)0}h^0$, $\bar{D}^0 \rightarrow K_S^0\pi^+\pi^-$ decays. The Dalitz plot is divided into 16 bins ($2\mathcal{N}$ in the general case) symmetrically with respect to $m_+^2 \leftrightarrow m_-^2$ exchange. The bin index i lies between -8 and 8 , excluding 0; $m_+^2 \leftrightarrow m_-^2$ exchange corresponds to the sign inversion $i \rightarrow -i$.

Several parameters related to a Dalitz plot bin on the Dalitz plane \mathcal{D} are introduced. These are the probability for the \bar{D}^0 meson to decay into the phase space region \mathcal{D}_i of the Dalitz plot bin i

$$K_i = \int_{\mathcal{D}_i} |\mathcal{A}_D(m_-^2, m_+^2)|^2 dm_+^2 dm_-^2, \quad (6)$$

(normalized by $\sum_{i=-8}^8 K_i = 1$) and the weighted averages of the sine and cosine of the phase difference between \bar{D}^0 and D^0 decay amplitudes $\Delta\delta_D(m_+^2, m_-^2)$ over the i -th Dalitz plot bin:

$$\begin{aligned} C_i &= \frac{\int_{\mathcal{D}_i} |\mathcal{A}_D| |\bar{\mathcal{A}}_D| \cos \Delta\delta_D dm_+^2 dm_-^2}{\sqrt{K_i K_{-i}}}, \\ S_i &= \frac{\int_{\mathcal{D}_i} |\mathcal{A}_D| |\bar{\mathcal{A}}_D| \sin \Delta\delta_D dm_+^2 dm_-^2}{\sqrt{K_i K_{-i}}}. \end{aligned} \quad (7)$$

The binning method yields the relations $C_i = C_{-i}$ and $S_i = -S_{-i}$. Eq. (1) can be expressed in the form appropriate for a time-dependent binned analysis:

$$\begin{aligned} \mathcal{P}_i(\Delta t, \varphi_1) &= h_2 e^{-\frac{|\Delta t|}{\tau_B}} \left[1 + q_B \frac{K_i - K_{-i}}{K_i + K_{-i}} \cos(\Delta m_B \Delta t) \right. \\ &\quad \left. + 2q_B \xi_{h^0}(-1)^L \frac{\sqrt{K_i K_{-i}}}{K_i + K_{-i}} \sin(\Delta m_B \Delta t) (S_i \cos 2\varphi_1 + C_i \sin 2\varphi_1) \right], \end{aligned} \quad (8)$$

where $q_B = -1$ (+1) corresponds to a signal B^0 (\bar{B}^0) meson and h_2 is a normalizing constant.

The knowledge of the signal-event distribution over the Dalitz plot bins for both B meson flavors is necessary for the fit that extracts the CP violation parameters. The expected fraction n_{i,q_B} of signal events for the i -th Dalitz plot bin and signal B flavor q_B is

$$n_{i,q_B} = \frac{K_i + K_{-i}}{2} + \frac{q_B}{1 + (\tau_B \Delta m_B)^2} \cdot \frac{K_i - K_{-i}}{2}. \quad (9)$$

This formula is obtained by integrating Eq. (8) over Δt .

In principle, each pair $(i, -i)$ of bins provides enough information to measure the CP violation parameters if the values of parameters $K_{\pm i}$, C_i , and S_i are known and do not equal zero.

For a given binning of the Dalitz plot, the parameters K_i can be measured with a set of flavor-tagged neutral D mesons such as $D^{*+} \rightarrow D^0\pi^+$ or $B^+ \rightarrow \bar{D}^0\pi^+$ decays, by measuring signal yield in each Dalitz plot bin. The measurement of the phase parameters C_i and S_i is more complicated and can be done with coherent decays of $D^0\bar{D}^0$ pairs [21].

Measurement of the CP violation parameters is possi-

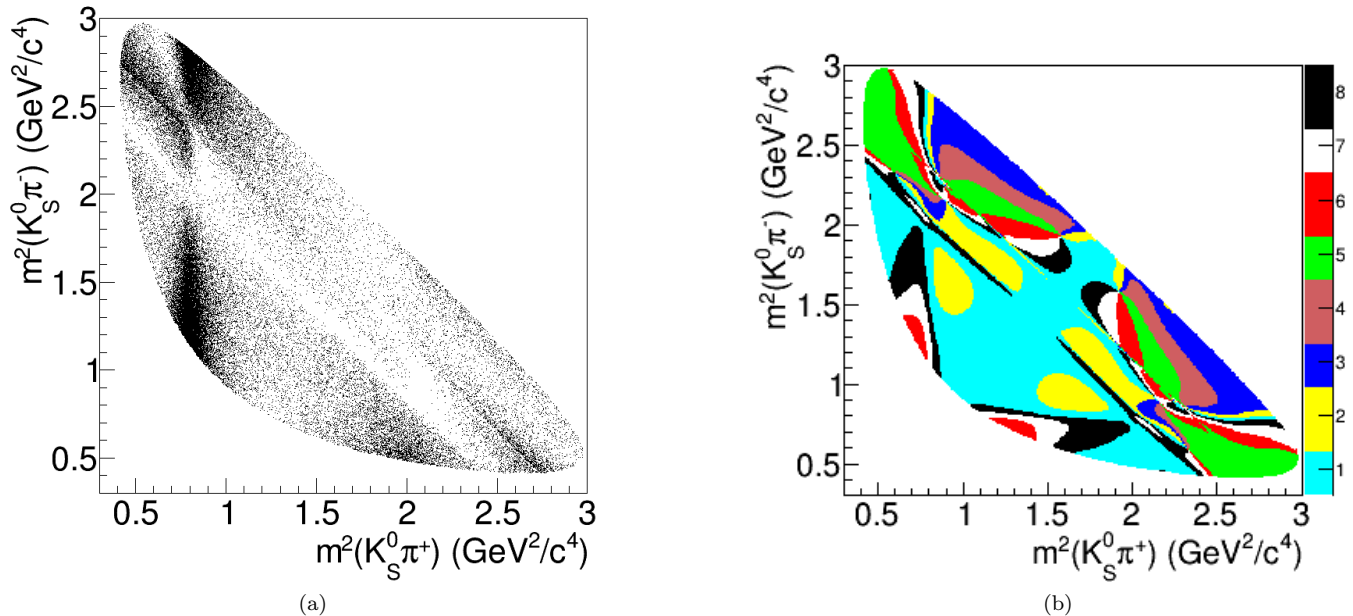


FIG. 2. Dalitz plot distribution (a) and equal-phase binning (b) obtained with the amplitude model of $\bar{D}^0 \rightarrow K_S^0 \pi^+ \pi^-$ decay from Ref. [20].

ble for an arbitrary binning of the Dalitz plot, but usage of the realistic decay amplitude model allows one to optimize the binning to approach the maximal statistical sensitivity. In particular, the equal-phase binning method [17] suggests the following rule for $i > 0$ and $m_+^2 < m_-^2$:

$$\frac{\pi(i-3/2)}{4} < \Delta\delta_D(m_+^2, m_-^2) < \frac{\pi(i-1/2)}{4}. \quad (10)$$

This binning and the $D^0 \rightarrow K_S^0 \pi^+ \pi^-$ decay amplitude model reported in Ref. [20] (see Fig. 2) are employed in the analysis presented here. The analysis uses the values of K_i extracted from the $B^+ \rightarrow \bar{D}^0 \pi^+$ sample, as described in Section IV, and the values of C_i and S_i parameters measured by CLEO-c [21], as listed in Table I.

Model-inspired binning of the Dalitz plot does not lead to a bias in the measured parameters, because of the excellent invariant mass resolution of the detector. Therefore, an alternative binning derived from a model that parameterized the data poorly would only reduce the statistical sensitivity of the measurement.

II. BELLE DETECTOR

This measurement is based on a data sample that contains $772 \times 10^6 B\bar{B}$ pairs, collected with the Belle detector at the KEKB asymmetric-energy e^+e^- (3.5 on 8 GeV) collider [22] operated near the $\Upsilon(4S)$ resonance.

The Belle detector is a large-solid-angle magnetic spectrometer that consists of a silicon vertex detector (SVD) featuring the double-sided silicon strip devices, a 50-layer central drift chamber (CDC), an array of aerogel

TABLE I. The values of the parameters C_i and S_i measured by CLEO-c [21] for equal-phase Dalitz-plot binning according to the $\bar{D}^0 \rightarrow K_S^0 \pi^+ \pi^-$ decay model obtained in Ref. [20].

Bin	C_i	S_i
1	$0.710 \pm 0.034 \pm 0.038$	$-0.013 \pm 0.097 \pm 0.031$
2	$0.481 \pm 0.080 \pm 0.070$	$-0.147 \pm 0.177 \pm 0.107$
3	$0.008 \pm 0.080 \pm 0.087$	$0.938 \pm 0.120 \pm 0.047$
4	$-0.757 \pm 0.099 \pm 0.065$	$0.386 \pm 0.208 \pm 0.067$
5	$-0.884 \pm 0.056 \pm 0.054$	$-0.162 \pm 0.130 \pm 0.041$
6	$-0.462 \pm 0.100 \pm 0.082$	$-0.616 \pm 0.188 \pm 0.052$
7	$0.106 \pm 0.105 \pm 0.100$	$-1.063 \pm 0.174 \pm 0.066$
8	$0.365 \pm 0.071 \pm 0.078$	$-0.179 \pm 0.166 \pm 0.048$

threshold Cherenkov counters, a barrel-like arrangement of time-of-flight scintillation counters, and an electromagnetic calorimeter comprised of CsI(Tl) crystals located inside a super-conducting solenoid coil that provides a 1.5 T magnetic field. An iron flux-return located outside of the coil is instrumented to detect K_L^0 mesons and to identify muons. The detector is described in detail elsewhere [23]. Two inner detector configurations were used. A 2.0 cm radius beampipe and a 3-layer silicon vertex detector was used for the first sample of $152 \times 10^6 B\bar{B}$ pairs, while a 1.5 cm radius beampipe, a 4-layer silicon vertex detector and a small-cell inner drift chamber were used to record the remaining $620 \times 10^6 B\bar{B}$ pairs [24].

III. EVENT SELECTION

Six $B^0 \rightarrow \bar{D}^{(*)0}h^0$ decay modes, $\bar{D}^0\pi^0$, $\bar{D}^0\eta$, $\bar{D}^0\eta'$, $\bar{D}^0\omega$, $\bar{D}^{*0}\pi^0$, and $\bar{D}^{*0}\eta$, with subsequent decays $\bar{D}^0 \rightarrow K_S^0\pi^+\pi^-$, $\eta \rightarrow \gamma\gamma$ or $\pi^+\pi^-\pi^0$, $\omega \rightarrow \pi^+\pi^-\pi^0$, $\eta' \rightarrow [\gamma\gamma]\eta\pi^+\pi^-$, and $\bar{D}^{*0} \rightarrow \bar{D}^0\pi^0$, are used in this analysis. Only $\eta \rightarrow \gamma\gamma$ is considered for the $\bar{D}^0\eta'$ and $\bar{D}^{*0}\eta$ modes. Charged B -meson decay $B^+ \rightarrow \bar{D}^0\pi^+$ followed by $\bar{D}^0 \rightarrow K_S^0\pi^+\pi^-$ is used to measure the parameters K_i .

The charged pion candidates are selected from the reconstructed tracks and are required to have both z and $r\phi$ hits in at least one layer and at least one additional layer with a z hit. The impact parameters of the tracks with respect to the beam interaction point in the longitudinal and transverse projections are required to satisfy $|dz| < 5$ cm and $dr < 2$ cm, respectively. The transverse momentum p_t is required to be greater than 50 MeV/ c (100 MeV/ c) for pions produced in $D^0 \rightarrow K_S^0\pi^+\pi^-$ ($h^0 \rightarrow \pi^+\pi^-\pi^0$) decay. These requirements are not applied for the pions daughters of K_S^0 candidates.

The $K_S^0 \rightarrow \pi^+\pi^-$ candidates are reconstructed from two oppositely charged tracks using two artificial neural networks (NN). The first NN is trained to suppress the combinatorial background and fake tracks: it uses the track impact parameters with respect to the beam interaction point, the azimuthal angle between the K_S^0 momentum and the decay-vertex vectors, the distance between the tracks, the K_S^0 flight length in the x - y plane, the K_S^0 momentum, the distance between the beam interaction point and the tracks, the angle between the K_S^0 and a pion flight directions, the presence of the SVD hits and number of CDC hits on the tracks. The second NN is trained to suppress the background from $\Lambda \rightarrow p\pi^-$ decays: it uses the reconstructed mass with the lambda hypothesis, the absolute values of the track momenta, the track-momenta polar angles and the particle identification parameter distinguishing pions from protons. Further details of the procedure are described in Ref. [25]. The invariant mass of the selected candidates is required to be between 488.5 and 506.5 MeV/ c^2 . This mass interval, as well as any other mass interval used in the analysis (unless explicitly stated otherwise), correspond to ± 3 standard deviations from the nominal value.

The π^0 candidates are formed from photon pairs with an invariant mass between 115.7 and 153.7 MeV/ c^2 . The photon energy is required to be greater than 40 MeV. The energy of the π^0 candidate from $h^0 \rightarrow \pi^+\pi^-\pi^0$ ($h^0 = \eta$ and ω) decay must to be greater than 200 MeV.

The $\eta \rightarrow \gamma\gamma$ candidates are formed from photon pairs with an invariant mass between 530.0 and 573.7 MeV/ c^2 . The photon energy is required to be greater than 80 MeV.

The $h^0 \rightarrow \pi^+\pi^-\pi^0$ candidates, where $h^0 = \eta$ or ω , are formed from a π^0 candidate and two oppositely charged tracks with invariant mass between 537.6 and 557.4 MeV/ c^2 for η and between 760.4 and 803.9 MeV/ c^2 for ω . For the ω candidates, the absolute value of the cosine of the helicity angle θ_{hel} (the angle between the B^0 flight direction and the normal to the ω decay plane

in the ω rest frame) is required to be greater than 0.2.

The $\eta' \rightarrow \eta\pi^+\pi^-$ candidates are formed from a $\eta \rightarrow \gamma\gamma$ candidate and two oppositely charged tracks, both treated as pions. The invariant mass difference $\Delta m_\eta \equiv m(\eta') - m(\eta)$ is required to lie between 401.7 and 417.7 MeV/ c^2 .

The $D^0 \rightarrow K_S^0\pi^+\pi^-$ candidates are formed from a K_S^0 candidate and two oppositely charged tracks, both treated as pions, with an invariant mass between 1.8516 and 1.8783 GeV/ c^2 .

The $D^{*0} \rightarrow D^0\pi^0$ candidates are formed from a D^0 candidate and a neutral pion candidate. The invariant mass difference $\Delta m_D \equiv m(D^{*0}) - m(D^0)$ must lie between 140.2 and 144.2 MeV/ c^2 .

The selection of B^0 and B^\pm candidates is based on the variables $\Delta E = E_B^{\text{CM}} - E_{\text{beam}}^{\text{CM}}$, the energy difference between the signal B candidate and beam in the CM frame, and $M_{\text{bc}} = \sqrt{(E_{\text{beam}}^{\text{CM}}/c^2)^2 - (p_B^{\text{CM}}/c)^2}$, the beam-energy constrained mass of the signal B candidate. The candidates satisfying $|\Delta E| < 0.3$ GeV and $M_{\text{bc}} > 5.2$ GeV/ c^2 are retained for further analysis.

The vertex-constrained kinematic fit is applied to the signal and tagging B candidates and to the D^0 candidates. We require $\chi^2/\text{n.d.f.} < 500$ for the vertex-constrained fit of the D^0 meson candidates, where n.d.f. denotes the number of degrees of freedom.

When h^0 is a π^0 or $\eta \rightarrow \gamma\gamma$ candidate, the $B^0 \rightarrow \bar{D}^{(*)0}h^0$ decay has no charged particle originating from the primary B decay vertex. In this case, the B decay vertex is determined by projecting the D^0 -candidate trajectory onto the beam-interaction profile. The estimated longitudinal resolution σ_z of a such vertex, obtained from the fit, is required to be less than 0.5 mm. This requirement is also imposed on the tagging B -decay vertices obtained by projecting a single track onto the beam interaction profile.

The vertex-constrained kinematic fit for other signal B decay modes requires that the D candidate trajectory and the two tracks from the h^0 decay originate from a common vertex and applies the Gaussian constraints on the position of this vertex based on the geometry of the beam interaction profile. The requirements $\sigma_z < 0.2$ mm and $\chi^2/\text{n.d.f.} < 50$ for the vertex quality are imposed, where $\chi^2/\text{n.d.f.}$ is calculated without taking into account the beam interaction profile constraint. These requirements are also imposed on the tagging B decay vertices reconstructed with more than one track.

The vertex position for the tagging B candidate is determined from the kinematic fit of well-reconstructed tracks that are not assigned to the signal B candidate decay chain [26].

The momentum of the π^0 , K_S^0 , and $\eta \rightarrow \gamma\gamma$ candidates, with the invariant mass constrained to its nominal value [27], is used to improve the ΔE resolution. The momenta of the D^0 daughters obtained by a mass-constraint fit to the D^0 candidate are used to calculate the Dalitz variables.

The continuum background arising from $e^+e^- \rightarrow q\bar{q}$

(where $q = u, d, s, c$) events is suppressed with the procedure described in Refs. [28, 29] and with the BDT [30, 31] algorithm implemented within the TMVA [32] package.

The b flavor of the tagging B meson is identified from inclusive properties of particles that are not associated with the signal B candidate [33]. The tagging information is represented by two parameters: the b -flavor charge q and the purity r . The parameter r is an event-by-event, MC-determined flavor-tagging dilution factor that ranges from $r = 0$ for no flavor discrimination to $r = 1$ for unambiguous flavor assignment. The data are sorted into seven intervals of r . For events with $r > 0.1$, the wrong tag fractions for six r intervals, w_l ($l = 1, 2, \dots, 6$), and their differences between B^0 and \bar{B}^0 decays, Δw_l , are determined from semileptonic and hadronic $b \rightarrow c$ decays [34]. If $r \leq 0.1$, the wrong tag fraction is set to 0.5 and the tagging information is not used. The total effective tagging efficiency, $\varepsilon_{\text{eff}} = \sum(f_l \times (1 - 2w_l)^2)$, is 0.3, where f_l is the fraction of events in the category l . The parameter $Q_B = q_B(1 - 2w)/(1 - q_B\Delta w)$ is used instead of the parameter q_B , defined in Eq. (8), to account for the wrong tag.

The signal yields of $B^0 \rightarrow \bar{D}^{(*)0}h^0$ modes are obtained from an extended unbinned maximum likelihood fit of the ΔE - M_{bc} two dimensional distribution in the region $\Delta E \in (-0.15 \text{ GeV}, 0.30 \text{ GeV}) \cap M_{\text{bc}} \in (5.20 \text{ GeV}/c^2, 5.29 \text{ GeV}/c^2)$. The signal yield of $B^+ \rightarrow \bar{D}^0\pi^+$ events is obtained from an extended unbinned maximum likelihood fit of the ΔE distribution in the region $(-0.10 \text{ GeV}, 0.15 \text{ GeV})$ for $M_{\text{bc}} \in (5.272 \text{ GeV}/c^2, 5.287 \text{ GeV}/c^2)$.

The sideband region is defined as the union of two rectangular regions in the ΔE - M_{bc} plane: $M_{\text{bc}} \in (5.23 \text{ GeV}/c^2, 5.26 \text{ GeV}/c^2) \cap \Delta E \in (-0.15 \text{ GeV}, 0.30 \text{ GeV})$ and $M_{\text{bc}} \in (5.26 \text{ GeV}/c^2, 5.29 \text{ GeV}/c^2) \cap \Delta E \in (0.12 \text{ GeV}, 0.30 \text{ GeV})$.

The selection criteria and the analysis procedure are tested using the Monte Carlo (MC) simulation and fixed before performing the fit of the CP violation parameters. The MC events are generated with EvtGen [35]. Final-state radiation from charged particles is simulated during the event generation using PHOTOS [36]. The generated events are processed through the detailed detector simulation based on GEANT3 [37].

IV. $B^+ \rightarrow \bar{D}^0\pi^+$ SAMPLE

The $B^+ \rightarrow \bar{D}^0\pi^+$ control sample is experimentally clean and has kinematic properties and detection efficiency similar to the $B^0 \rightarrow \bar{D}^{(*)0}h^0$ decay. We use this process to select a sample of D mesons in the flavor eigenstate and to measure the parameters K_i defined in Eq. (6).

A. Signal yield

Three components are included in the fit of the ΔE distribution: signal, $B^+ \rightarrow \bar{D}^0K^+$ background and combinatorial background.

The signal distribution is parameterized by the sum of a Gaussian and two Crystal Ball functions [38] with a common peak position. The mean and the Gaussian width are free fit parameters while the other parameters are fixed to the values obtained from simulation. Background from the $B^+ \rightarrow \bar{D}^0K^+$ decays is parameterized by a Gaussian function with all parameters fixed from simulation. Combinatorial background is parameterized by a second-order Chebyshev polynomial. The parameters of the combinatorial background shape are obtained from the fit. The ΔE distribution for $B^+ \rightarrow \bar{D}^0\pi^+$ candidates and the results of the fit are shown in Fig. 3. Yields of the signal and background components are listed in Table II.

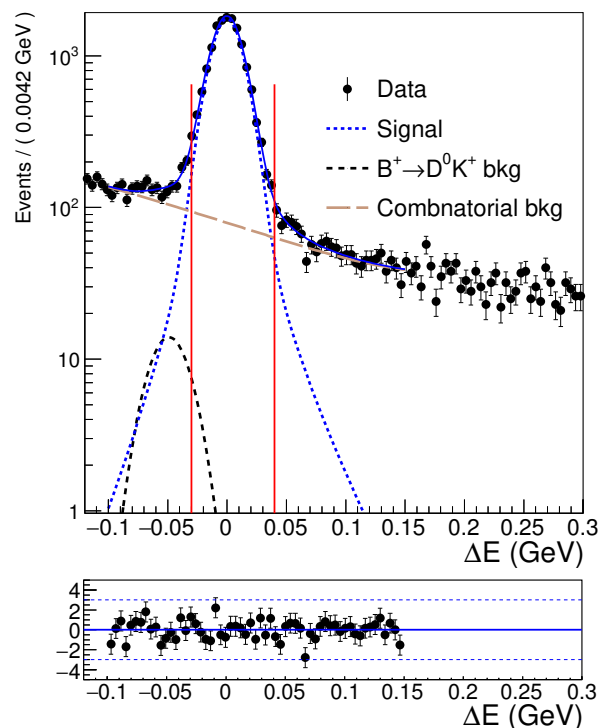


FIG. 3. ΔE distribution for $B^+ \rightarrow \bar{D}^0\pi^+$ candidates. Black circles with error bars show data, the solid blue line is the complete fit function, the dashed blue line is the signal component, the dashed black line is the background from $B^+ \rightarrow \bar{D}^0K^+$ decays, the dashed brown line is the combinatorial background. Vertical red lines show the signal area. Histogram with the pulls of the data with respect to the fit curve is shown at the bottom (with horizontal blue dashed lines at pull values of ± 3).

The parameters K_i are measured using the events in the ΔE interval between -30 and 40 MeV. This interval is optimized to suppress the background from

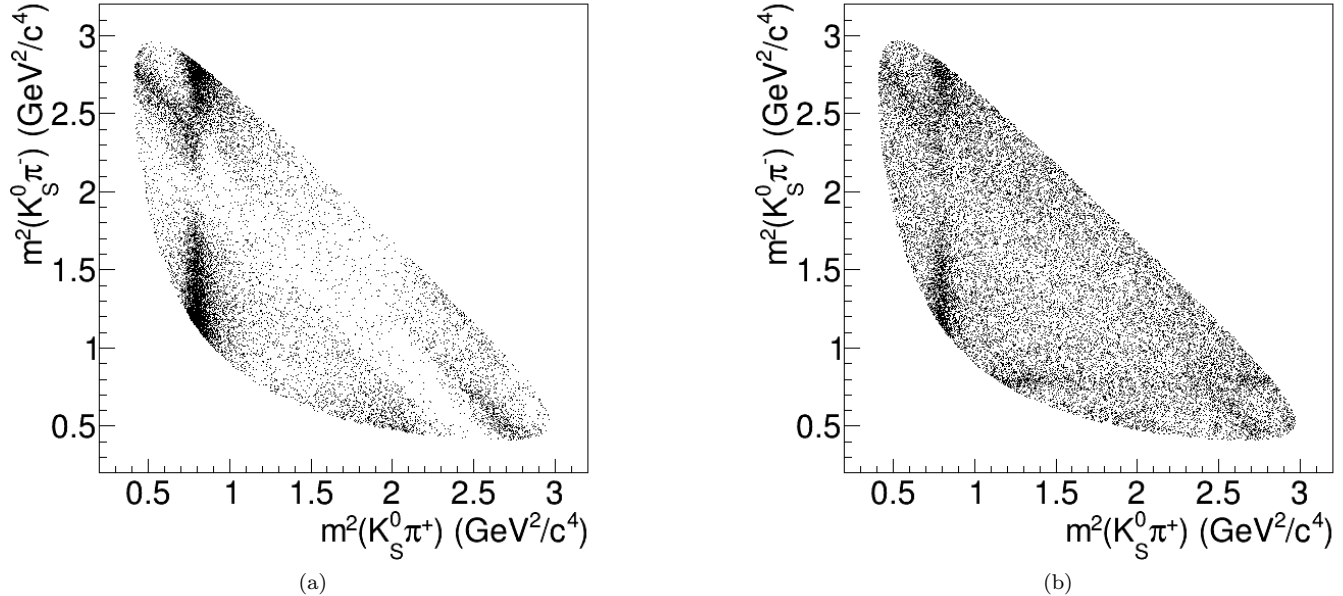


FIG. 4. Dalitz plot distributions for $D \rightarrow K_S^0 \pi^+ \pi^-$ candidates with D from $B^+ \rightarrow \bar{D}^0 \pi^+$ decay in the signal (a) and sideband (b) areas.

TABLE II. Fit results of the ΔE distribution for $B^+ \rightarrow \bar{D}^0 \pi^+$ candidates. The numbers of events and the fraction of signal events are shown for the signal ΔE region.

Parameter	Value
Signal yield	$(1.375 \pm 0.014) \times 10^4$
$B^+ \rightarrow \bar{D}^0 K^+$ yield	18.7 ± 9.8
Combinatorial bkg. yield	1295 ± 79
Signal fraction (%)	91.3 ± 0.9

$B^+ \rightarrow \bar{D}^0 K^+$ events without significant signal-efficiency loss.

B. Measurement of parameters K_i

The charged pion from the $B^+ \rightarrow \bar{D}^0 \pi^+$ decay tags the flavor of the D meson. Therefore, the fraction of the signal events corresponding to the i -th Dalitz plot bin equals K_i .

The Dalitz distribution for $D \rightarrow K_S^0 \pi^+ \pi^-$ in the signal ΔE range, where the D meson is produced in $B^+ \rightarrow \bar{D}^0 \pi^+$ decays, is shown in Fig. 4a. The fraction of signal, $f_{\text{sig}} = (91.3 \pm 0.9)\%$, is obtained from a fit of the ΔE distribution. The Dalitz plot for events from the ΔE - M_{bc} sideband is shown in Fig. 4b. The binned background distribution is obtained from this data.

The values of the parameters K_i are listed in Table III. The uncertainties shown include the statistical uncertainty of the signal sample and the uncertainty due to background evaluation, added in quadrature. The

TABLE III. The values of the parameters K_i measured with the $B^+ \rightarrow \bar{D}^0 \pi^+$ data sample. The values are not corrected for the detection efficiency.

Bin (i)	K_i (%)	K_{-i} (%)
1	17.42 ± 0.32	7.81 ± 0.25
2	7.51 ± 0.22	1.29 ± 0.10
3	10.24 ± 0.26	2.58 ± 0.14
4	2.85 ± 0.14	1.16 ± 0.10
5	9.45 ± 0.25	4.25 ± 0.17
6	7.31 ± 0.22	1.73 ± 0.11
7	10.48 ± 0.26	1.18 ± 0.10
8	12.46 ± 0.28	2.38 ± 0.14

systematic uncertainties associated with the background Dalitz plot distribution are neglected because the background fraction is very small.

V. $B^0 \rightarrow \bar{D}^{(*)0} h^0$ SAMPLE

A. Background components

Three background components are considered for the $B^0 \rightarrow \bar{D}^{(*)0} h^0$ candidates:

- combinatorial background from non-resonant light quark production (continuum background);
- combinatorial background from $B\bar{B}$ events; and
- background from partially reconstructed B decays.

Background from partially reconstructed decays is dominated by $B \rightarrow \bar{D}^0 \rho$ and $B \rightarrow \bar{D}^* \pi^0$ for the $B^0 \rightarrow \bar{D}^0 \pi^0$ mode and by $B \rightarrow \bar{D}^* \rho$ for the $B^0 \rightarrow \bar{D}^{*0} \pi^0$ mode. These processes, reconstructed with one missing pion, lead to a concentration below -0.1 GeV in the ΔE distribution. The background in all other channels is dominated by the combinatorial contribution with featureless ΔE distribution.

The background contribution from charmless B^0 decays is suppressed by requiring the presence of a D^0 candidate and thus is found to be negligible in this measurement.

B. Signal yield

A two-dimensional unbinned maximum likelihood fit of the ΔE - M_{bc} distribution is performed for each signal mode. The probability density function (PDF) contains four components, corresponding to the signal and three backgrounds introduced above.

The signal ΔE distributions are parameterized by the sum of a Gaussian and two Crystal Ball functions with a common peak position. The signal M_{bc} distributions are parameterized by a function introduced in Ref. [39] and referred to as the Novosibirsk distribution. The peak position in the ΔE - M_{bc} plane is obtained from the fit while the other parameters are fixed at the values obtained from simulation.

The ΔE distributions for events from continuum background are parameterized by a second-order Chebyshev polynomial. The ΔE distributions of the combinatorial background from the $B\bar{B}$ events are parameterized by an exponential function. The M_{bc} distributions of the combinatorial backgrounds are parameterized by an ARGUS function [40]. The parameters of the ΔE PDF are obtained from the fit while those of the M_{bc} PDF are fixed at the values obtained from simulation.

The ΔE distributions of the background from partially reconstructed B decays are parameterized by the following function:

$$p_{\text{pr}}(\Delta E) \propto 1 + \zeta_1 (\Delta E - \Delta E_0) + s \ln \left(1 + b \exp \left[\frac{(\zeta_r - \zeta_1) (\Delta E - \Delta E_0)}{s} \right] \right). \quad (11)$$

This function describes two asymptotically straight lines smoothly merged near the point given by the ΔE_0 parameter whose slopes are given by $\zeta_{\{r,1\}}$. The parameter s determines the curvature at the junction. If the B candidate decay chain contains a π^0 or η reconstructed in the $\gamma\gamma$ final state, the M_{bc} distribution of the background from partially reconstructed B decays is parameterized by the Novosibirsk function; otherwise, it is parameterized by the sum of ARGUS and Gaussian functions. All parameters are fixed at the values obtained from simulation except for the values of the ΔE_0 parameter for the $B^0 \rightarrow \bar{D}^0 \pi^0$ and $B^0 \rightarrow \bar{D}^{*0} \pi^0$ modes that are obtained from the fit.

Several correlations between the ΔE and M_{bc} distributions are taken into account. A left-side tail of the signal ΔE distribution is due to π^0 or η candidate where only one photon was identified correctly. This partially wrong combination leads to correlated shift both in ΔE and M_{bc} . A similar correlation appears in the distributions of the background from partially reconstructed B decays. The width of the signal ΔE distribution for the B candidates with the η or ω reconstructed in the $\pi^+ \pi^- \pi^0$ final state is determined by the charged final state particles momentum resolution if both final state photons are correctly assigned. For such candidates, the ΔE and M_{bc} distributions are correlated. That correlation is accommodated by introducing a ΔE dependence of the signal M_{bc} PDF parameters. This parameterization is equivalent to a two-dimensional Gaussian function. No significant correlation is found for the combinatorial background. The values of parameters required to employ the correlations are obtained from simulation.

The fit projections for the $B^0 \rightarrow \bar{D}^0 \pi^0$ and $B^0 \rightarrow \bar{D}^0 \omega$ modes are shown in Fig. 5. The fit projections for the other signal modes are shown in Fig. 6. The fractions of background from partially reconstructed B decays are small for all modes except $B^0 \rightarrow \bar{D}^0 \pi^0$ and $B^0 \rightarrow \bar{D}^{*0} \pi^0$ (compare the ΔE distributions below -0.1 GeV for $B^0 \rightarrow \bar{D}^0 \pi^0$ and $B^0 \rightarrow \bar{D}^0 \omega$ in Fig. 5, for example) and cannot be determined from the fit. These fractions are fixed relative to the fractions of combinatorial background from $B\bar{B}$ events using the values obtained from MC simulation.

TABLE IV. Results of the ΔE - M_{bc} fit for $B^0 \rightarrow \bar{D}^{(*)0} h^0$ data. The numbers of events N_{sig} and the fractions f_{sig} of signal events obtained from the fit for the signal ΔE - M_{bc} regions are shown.

Mode	N_{sig}	f_{sig} (%)
$B^0 \rightarrow \bar{D}^0 \pi^0$	464 ± 26	72.1 ± 4.1
$B^0 \rightarrow \bar{D}^0 \eta_{\gamma\gamma}$	99 ± 14	50.5 ± 7.0
$B^0 \rightarrow \bar{D}^0 \eta_{\pi^+ \pi^- \pi^0}$	51.3 ± 8.8	66 ± 11
$B^0 \rightarrow \bar{D}^0 \omega$	182 ± 18	58.4 ± 5.7
$B^0 \rightarrow \bar{D}^0 \eta'$	28.2 ± 6.4	70 ± 16
$B^0 \rightarrow \bar{D}^{*0} \pi^0$	103 ± 17	44.1 ± 7.4
$B^0 \rightarrow \bar{D}^{*0} \eta$	36.1 ± 7.6	64 ± 13
Total	962 ± 41	61 ± 2.6

The ellipses in the ΔE - M_{bc} plane inscribed in the rectangular areas marked by the vertical red lines in Figs. 5 and 6 are defined for each signal mode and are referred to as signal regions. The events in these signal regions are used in the fit of the CP violation parameters. The signal yields N_{sig} and fractions f_{sig} of signal events for each signal region obtained from the ΔE - M_{bc} fit, are listed in Table IV. The Dalitz plots for events with a wrong-tag probability of under 23% are shown in Fig. 7.

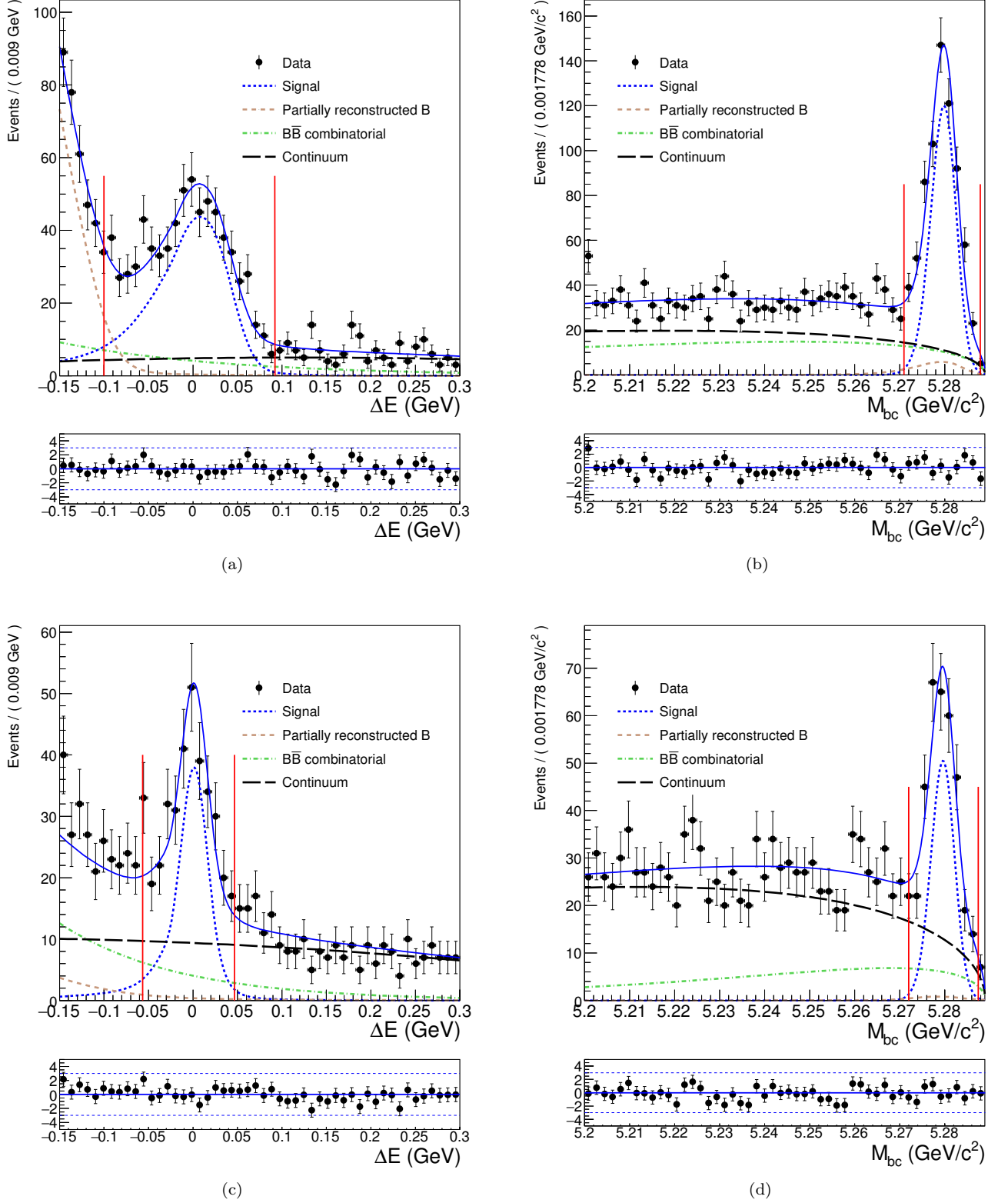


FIG. 5. ΔE fit projections for the signal M_{bc} regions (a, c) and M_{bc} fit projections for the signal ΔE regions (b, d) for the $B^0 \rightarrow \bar{D}^0 \pi^0$ (a, b) and $B^0 \rightarrow \bar{D}^0 \omega$ (c, d) candidates. Black circles with errors show data, continuous blue lines show projections of complete fit functions, dashed blue lines show signal components, dashed black lines show continuum background components, dashed brown lines show background from partially reconstructed B decays and dot-dashed lines show combinatorial background from $B\bar{B}$ events. Histograms with the pulls of the data with respect to the fit curves are shown at the bottom of each plot (with horizontal blue dashed lines at pull values of ± 3).

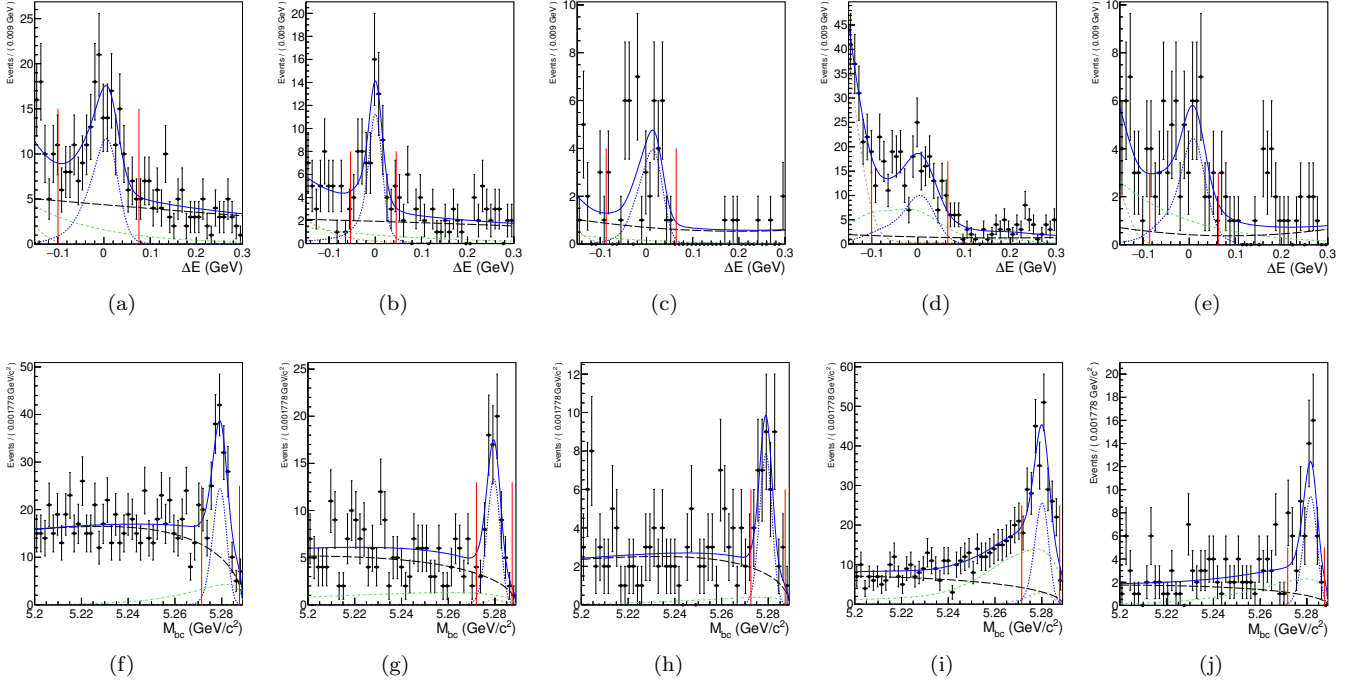


FIG. 6. ΔE fit projections for the signal M_{bc} regions (a–e) and M_{bc} fit projections for the signal ΔE regions (f–j) for the $B^0 \rightarrow \bar{D}^0 \eta$, $\eta \rightarrow \gamma\gamma$ (a, f), $B^0 \rightarrow \bar{D}^0 \eta$, $\eta \rightarrow \pi^+ \pi^- \pi^0$ (b, g), $B^0 \rightarrow \bar{D}^0 \eta'$ (c, h), $B^0 \rightarrow \bar{D}^{*0} \pi^0$ (d, i), and $B^0 \rightarrow \bar{D}^{*0} \eta$ (e, j) candidates. Black circles with errors show data, continuous blue lines show projections of complete fit functions, dashed blue lines show signal components, dashed black lines show continuum background components, dashed brown lines show background from partially reconstructed B decays and dot-dashed lines show combinatorial background from $B\bar{B}$ events.

VI. DETERMINATION OF THE CP VIOLATION PARAMETERS

The CP violation parameters are measured using the unbinned maximum likelihood fit of the Δt distribution. The likelihood function is defined as

$$\mathcal{L} = \prod_{j=1}^N [(1 - f_{\text{bkg},j}) p_{\text{sig}}(\Delta t_j) + f_{\text{bkg},j} p_{\text{bkg}}(\Delta t_j)], \quad (12)$$

where the product is evaluated over all N events in the sample, $f_{\text{bkg},j}$ is the event-dependent background fraction obtained from the ΔE – M_{bc} fit, p_{sig} is the signal PDF, and p_{bkg} is the background PDF.

The background Δt distributions are parameterized by convolving the function

$$f_{\delta} \delta(\Delta t) + (1 - f_{\delta}) 2\tau_{\text{bkg}} e^{-|\Delta t|/\tau_{\text{bkg}}} \quad (13)$$

with a double-Gaussian function; here, δ is the Dirac delta function and τ_{bkg} is the effective lifetime for background events. The widths of the double-Gaussian function are event-dependent and proportional to the estimated vertex resolution obtained from the vertex-constrained kinematic fits. The parameters f_{δ} and τ_{bkg} are obtained from simulation while the parameters of the double-Gaussian function are obtained from the fit of the

Δt distribution in the ΔE – M_{bc} sideband. The Δt distributions for background from $B\bar{B}$ events and from continuum events are parameterized separately.

The signal Δt distribution is parameterized by convolving Eq. (8) with a resolution function. The resolution function is described in Ref. [41]. It is tuned for each event using information obtained from the vertex-constrained kinematic fits.

Table V shows results of the fit of the CP violation parameters, where $\sin 2\varphi_1$ and $\cos 2\varphi_1$ are treated as independent variables. The correlation coefficient of $\sin 2\varphi_1$ and $\cos 2\varphi_1$ is about -3% .

TABLE V. Fit of the CP violation parameters. Only statistical uncertainty is shown.

Signal mode	$\sin 2\varphi_1$	$\cos 2\varphi_1$
$B^0 \rightarrow \bar{D}^0 \pi^0$	0.61 ± 0.37	$0.88^{+0.46}_{-0.52}$
$B^0 \rightarrow \bar{D}^0 \omega$	-0.12 ± 0.58	$1.28^{+0.62}_{-0.69}$
Other modes	0.44 ± 0.51	$0.89^{+0.49}_{-0.55}$
All modes	0.41 ± 0.27	0.97 ± 0.33

The combined fit of all signal modes, with the parameters $\sin 2\varphi_1$ and $\cos 2\varphi_1$ considered as functions of the angle φ_1 , results in

$$\varphi_1 = 11.7^\circ \pm 7.8^\circ (\text{stat.}). \quad (14)$$

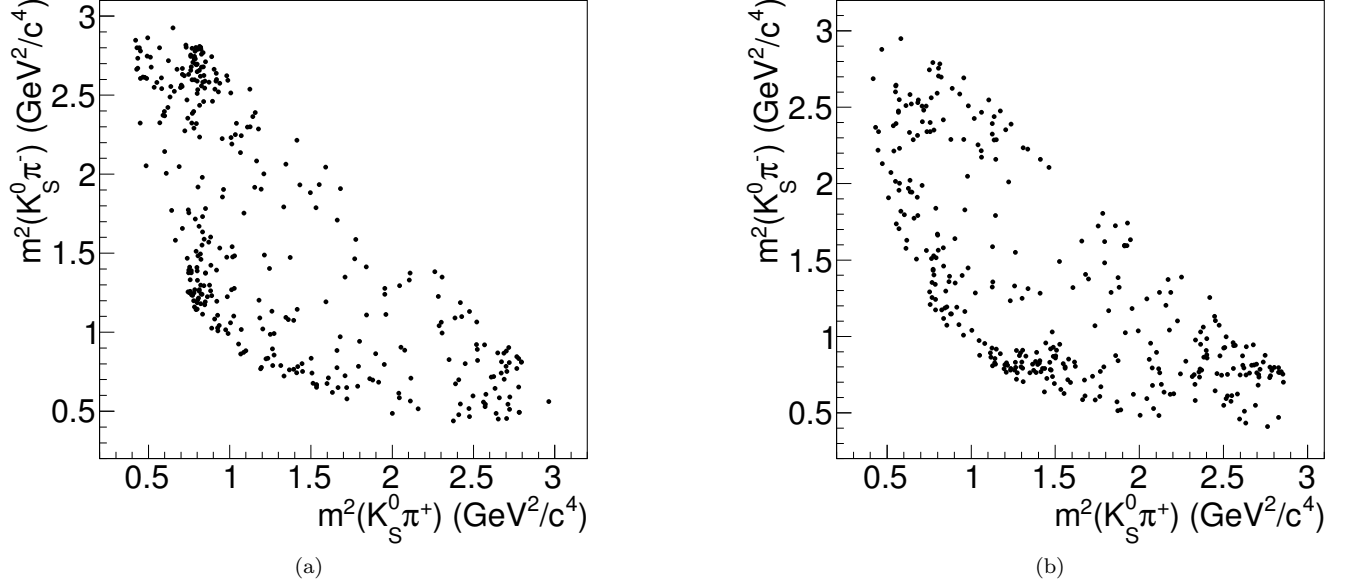


FIG. 7. Dalitz distributions for D mesons produced in tagged $B^0 \rightarrow \overline{D}^{(*)0} h^0$ decays with wrong tag probability of less than 23%. The signal B meson is tagged as B^0 (a) and \overline{B}^0 (b).

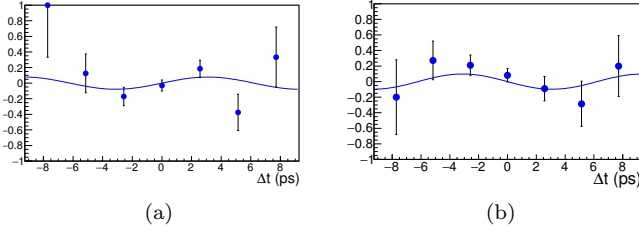


FIG. 8. Raw CP asymmetry distributions for the $B^0 \rightarrow \overline{D}^{(*)0} h^0$ candidates in the ± 1 -st (a) and ± 5 -th (b) $D \rightarrow K_S^0 \pi^+ \pi^-$ decay Dalitz plot bins. Red lines are the result of the CP violation fit performed with the full data sample. The asymmetry for the $B^0 \rightarrow \overline{D}^{*0} h^0$ candidates is taken with inverted sign.

For illustration, the raw CP asymmetries for the Dalitz plot bins most sensitive to $\sin 2\varphi_1$ are shown in Fig. 8. The Δt distributions for the Dalitz plot bins most sensitive to $\cos 2\varphi_1$ are shown in Fig. 9.

VII. SYSTEMATIC UNCERTAINTIES

Table VI provides the estimates of the systematic uncertainties in the measured values of the CP violation parameters.

The uncertainty due to the experimental resolution for the Dalitz variables is evaluated using the large sample of simulated signal events. The fit results are compared for the the CP violation fit performed using the reconstructed and the generated Dalitz-variables values. The

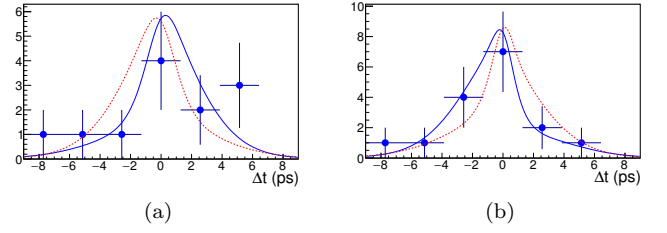


FIG. 9. Δt distributions for the $B^0 \rightarrow \overline{D}^0 h^0$ candidates with wrong-tag probability of less than 23%. (a) ((b)) corresponds to the candidates from the -3 -th (7 -th) $D \rightarrow K_S^0 \pi^+ \pi^-$ Dalitz plot bin tagged as B^0 (\overline{B}^0). Continuous blue lines are the result of the CP violation fit performed with the full data sample. Dashed red lines are obtained with $\varphi_1 = 68.1^\circ$.

uncertainty due to the detection-efficiency variation over the Dalitz plot is also evaluated using the simulated signal events. The fit results are compared for the CP violation fit performed with and without the efficiency correction.

The systematic uncertainty related to the signal Δt parameterization is estimated by varying each resolution parameter by $\pm\sigma_\pm$ ($\pm 2\sigma_\pm$ for parameters obtained from MC simulation) and repeating the fit.

Other contributions to the systematic uncertainty (items 4–10 in Table VI) are evaluated simultaneously from the fit performed with *nuisance* parameters and the

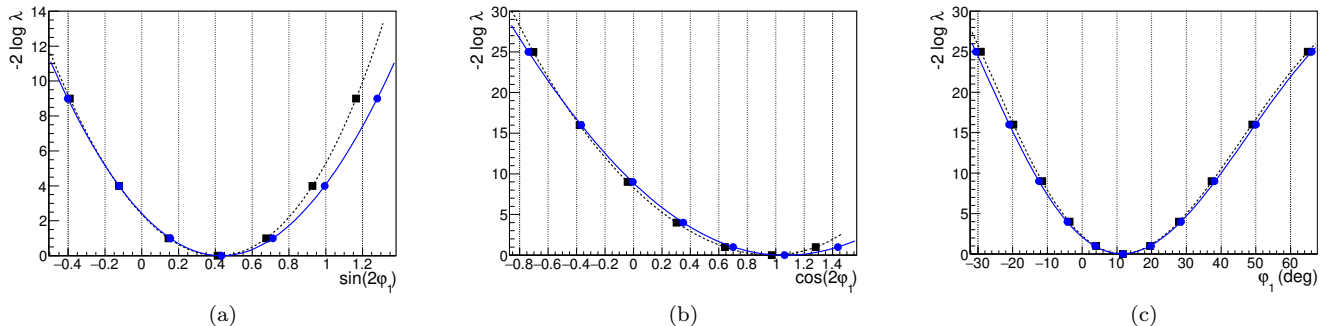


FIG. 10. Negative double logarithm of profiled likelihood ratio Eq. (16) for $\sin 2\varphi_1$ (a), $\cos 2\varphi_1$ (b) and φ_1 (c) obtained with the Minos algorithm [42]. Black squares mark $n\sigma$ standard confidence intervals corresponding to statistical uncertainty while blue circles mark $n\sigma$ standard confidence intervals corresponding to the overall uncertainty. Continuous blue and dashed black lines show 4-th (a), (b) and 5-th order (c) polynomial fit.

likelihood function expressed as follows:

$$-2 \log \mathcal{L}_n = -2 \log \mathcal{L} + \sum_{j,k} (p_j - p_j^0) \mathcal{K}_{jk} (p_k - p_k^0), \quad (15)$$

where \mathcal{L} is defined in Eq. (12), p_j and p_j^0 are the current and central values of the j -th nuisance parameter, respectively, \mathcal{K} is the inverse covariance matrix for the nuisance parameters and the sum is evaluated over all nuisance parameters. The following nuisance parameters are introduced to evaluate the systematic uncertainty:

- the parameters C_i and S_i that give the dominant contribution (with the covariance matrix taken from the supplementary materials for Ref. [21]).
- the parameters K_i with the uncertainties shown in Table III;
- the yield of signal events in each Dalitz plot bin for each signal mode with the value and uncertainty obtained from the $\Delta E - M_{bc}$ fit;
- the background Δt PDF parameters with the values and uncertainties obtained from the fit of the Δt distribution in the $\Delta E - M_{bc}$ sideband;
- the parameters τ_B and Δm_B with values and uncertainties taken from Ref. [43]; and
- the average bias in the wrong-tag probability with the uncertainty obtained using the results from Ref. [34].

The flavor tagging procedure and the uncertainties in the Δm_B and τ_B values give negligible contributions to the systematic uncertainty.

Frequentist confidence intervals for the CP violation parameters are evaluated using the profile likelihood method with likelihood ratios [44]

$$\lambda(\xi) = \frac{\mathcal{L}(\xi, \hat{p})}{\mathcal{L}(\hat{\xi}, \hat{p})}, \quad (16)$$

where ξ is $\sin 2\varphi_1$ or $\cos 2\varphi_1$ or φ_1 , $\hat{\xi}$ is the optimal value, \hat{p} represents the optimal values of all other parameters corresponding to $\hat{\xi}$, and \hat{p} represents the optimal values of all other parameters corresponding to the ξ value. Negative double logarithms of the likelihood ratios are shown in Fig. 10.

TABLE VI. The sources and estimates of the systematic uncertainties for the CP violation parameters measured in the $B^0 \rightarrow \bar{D}^{(*)0} h^0$ decays. The uncertainty σ_{nuis} due to the sources 4–10 is evaluated from the single fit varying all the nuisance parameters and using the likelihood function Eq. (15). The total systematic uncertainty σ_{syst} is calculated as $\sqrt{\sigma_1^2 + \sigma_2^2 + \sigma_3^2 + \sigma_{\text{nuis}}^2}$. The values related to the sources 4–10 are shown for illustration.

Source	$\delta_{\sin 2\varphi_1}$ (%)	$\delta_{\cos 2\varphi_1}$ (%)	δ_{φ_1} (deg)
1. Dalitz variables resol.	0.3	0.7	0.1
2. Detection efficiency	0.6	0.8	0.2
3. Δt resolution	3.8	6.7	1.2
4. Flavor tagging	0.1	0.1	< 0.1
5. Δm_B	0.1	0.1	< 0.1
6. τ_B	0.1	0.1	< 0.1
7. $M_{bc} - \Delta E$ fit	3.4	1.9	0.8
8. Bkg. Δt param.	3.6	3.1	0.7
9. K_i	3.2	2.0	0.7
10. C_i and S_i	7.6	$^{+20}_{-13}$	1.1
σ_{nuis}	7.6	$^{+20}_{-13}$	1.6
Total σ_{syst}	8.5	$^{+21}_{-15}$	2.1
Stat. error for comparison	27	33	7.8

The dominant uncertainties shown in Table VI could be reduced in high-statistics measurements at Belle II. Indeed, the uncertainties associated with the parameters K_i , the Δt parameterization and the $\Delta E - M_{bc}$ fit are determined by the size of the data sample. The parameters C_i and S_i can be measured more precisely with a large data set of coherently produced $D^0 \bar{D}^0$ pairs collected by the BES-III experiment.

VIII. CONCLUSIONS

A novel model-independent approach for measuring the CKM angle φ_1 has been developed and applied to the full data set of the Belle experiment. The following results are obtained:

$$\begin{aligned}\sin 2\varphi_1 &= 0.43 \pm 0.27 \text{ (stat.)} \pm 0.08 \text{ (syst.)}, \\ \cos 2\varphi_1 &= 1.06 \pm 0.33 \text{ (stat.)}_{-0.15}^{+0.21} \text{ (syst.)}, \\ \varphi_1 &= 11.7^\circ \pm 7.8^\circ \text{ (stat.)} \pm 2.1^\circ \text{ (syst.)}.\end{aligned}\quad (17)$$

The value $\sin 2\varphi_1 = 0.691 \pm 0.017$ measured in $b \rightarrow c\bar{c}s$ transitions determines the absolute value of $\cos 2\varphi_1$ leading to two possible solutions in the $0^\circ \leq \varphi_1 < 180^\circ$ range. Our measurement is inconsistent with the negative solution corresponding to the value $\varphi_1 = 68.1^\circ$ at the level of 5.1 standard deviations but in agreement with the positive solution corresponding to the value $\varphi_1 = 21.9^\circ$ at 1.3 standard deviations. Thus, this measurement clearly resolves the ambiguity in φ_1 inherent in the measurement of $\sin 2\varphi_1$ using the $b \rightarrow c\bar{c}s$ transition.

This measurement supersedes the previous measurement of the $\sin 2\varphi_1$ and $\cos 2\varphi_1$ in $B^0 \rightarrow \bar{D}^{(*)0}h^0$ decays at Belle [8]. Nevertheless, it should be emphasized that a different analysis technique is used here. Furthermore, experimental information from $B^+ \rightarrow \bar{D}^0\pi^+$ decays and from Ref. [21] is used in this analysis but not in Ref. [8].

The binned Dalitz plot approach could be used for precise φ_1 measurements in $B^0 \rightarrow \bar{D}^{(*)0}h^0$ followed by $\bar{D}^0 \rightarrow K_S^0\pi^+\pi^-$ decays with the high-statistics data from the Belle II experiment. The dominant systematic uncertainties could be reduced with this larger data sample. Also, abundant coherently-produced $D^0\bar{D}^0$ pairs collected by the BES-III experiment can be used to improve our knowledge of the phase parameters C_i and S_i . The number of Dalitz plot bins can be increased in future measurements to improve the statistical sensitivity to the CP violation parameters.

Some NP models predict the magnitude of CP violation to differ from the SM expectations [45]. The difference may vary for different quark transitions. Thus, it would be interesting to compare the $\sin 2\varphi_1$ value precisely measured in the $b \rightarrow c\bar{u}d$ transitions governing the $B^0 \rightarrow \bar{D}^{(*)0}h^0$ decays with the $\sin 2\varphi_1$ value precisely measured in the $b \rightarrow c\bar{c}s$ transitions.

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